

# **EXHIBIT 3**

UNITED STATES DISTRICT COURT  
MIDDLE DISTRICT OF NORTH CAROLINA

SHAUNA WILLIAMS, et al., )  
                            )  
                            )  
Plaintiffs,             )  
                            )  
                            )  
v.                         ) Civil Action No. 23 CV  
                            )  
                            ) 1057

REPRESENTATIVE DESTIN HALL,)  
in his official capacity as)  
Chair of the House Standing)  
Committee on Redistricting,)  
et al.,                     )  
                            )  
                            )  
Defendants.                )

----- )  
NORTH CAROLINA STATE     )  
CONFERENCE OF THE NAACP, )  
et al.,                     )  
                            )  
                            )  
Plaintiffs,                )  
                            )  
                            )  
v.                         ) Civil Action No. 23 CV  
                            )  
                            ) 1104

PHILIP BERGER, in his     )  
official capacity as the    )  
President Pro Tempore of   )  
the NORTH CAROLINA Senate, )  
et al.,                     )  
                            )  
                            )  
Defendants.                )

----- )

Videoconference deposition of MICHAEL BARBER, PhD,  
taken by counsel for the Plaintiffs, on Wednesday,  
October 30, 2024, beginning at 8:02 a.m. MDT.

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1           A     No, it did not. That's the main criticism that  
2       I have of his analysis, is that it lacks a measure of  
3       partisanship.

4           Q     And then you also state that you include a  
5       variable indicating if the precinct is located within the  
6       district's major city, and you say here, as identified by  
7       Dr. Rodden. So I take it that Dr. Rodden's regression  
8       analysis also included this variable?

9           A     In some cases, yes, and in other cases, no,  
10      but I tried to mirror as closely as possible what he did  
11      with regard to that variable.

12          Q     And then you also have a variable measuring the  
13      precinct's distance from the district's geographic center  
14      of population; was that variable included in Dr. Rodden's  
15      analysis?

16          A     Yes.

17          Q     Have you ever published a paper involving a  
18      regression model where two of the independent variables  
19      are correlated above 0.9?

20          A     I don't, off the top of my head, know if I have  
21      or have not. I would need to go back into the datasets  
22      and look.

23          Q     Are you familiar with the term  
24      multicollinearity?

25          A     Yes, I am.

1 Q What does it mean, in your field?

2 A It means the presence of correlation between  
3 two independent variables in a regression model.

4 Q Are party and race highly correlated in  
5 North Carolina?

6 A To varying degrees, yes. It's not constant  
7 across the state. It differs in different regions of  
8 the state.

9 Q Do you know how correlated it is in the areas  
10 where the challenged Congressional districts are?

11 A I could not tell you the numbers off the top of  
12 my head. I believe Dr. Rodden provides those in his  
13 reply report.

14 Q Okay. So let's look at page 7 of Dr. Rodden's  
15 reply report. So he notes at the top here, in  
16 Dr. Barber's VTD level dataset, the correlation between  
17 the Democratic vote share and BVAP is 0.85 in the  
18 envelope of District 6, 0.88 in the envelope of  
19 District 12, 0.82 in the envelope of District 14, and  
20 0.96 in the envelope of District 1; did you verify these  
21 correlations?

22 A No, I have not had time or reason, really, to  
23 dig into his replication data.

24 Q And you don't dispute -- or, sorry, do you have  
25 any reason to dispute them?

1 MS. RIGGINS: Objection.

2 THE WITNESS: I mean, I don't want to -- I  
3 don't know. I would need to look to verify them.  
4 I guess I'd have to say I just don't know.

5 Q But sitting here today, you don't have any  
6 basis to dispute them?

7 A No, I don't have any specific reason to dispute  
8 the numbers in this paragraph.

9 Q Would you agree that all of these levels of  
10 correlation are above 0.8?

11 A Yes, they are all above 0.8.

12 Q And one of them is very close to 1; it's 0.96?

13 A That is correct.

14 Q Would you agree that all of these are highly  
15 correlated?

16 A I think correlation is a continuous scale and  
17 I think we talked about a correlation a few hours ago  
18 that was moderately high. I think here we can say --  
19 maybe we can separate the ones in the 80s from the one  
20 that's 0.96 and I think we could all agree that 0.96 is  
21 very high. I think the ones in the 80s, we could say,  
22 are high. I think that it's -- correlation is a  
23 continuous measure and there's no definitively agreed  
24 upon threshold at which, you know, scholars would agree  
25 if something is high or low. It's a spectrum.

1           Q     Does including two highly correlated variables  
2       in the same regression change how the regression works?

3           A     It does not change how the regression works.  
4       Regardless of the correlation between the two independent  
5       variables, the regression does the same thing.

6           Q     Does including two highly correlated variables  
7       in the same regression impact the results of the  
8       regression analysis?

9           A     Any time you include an additional variable,  
10      it is going to have some correlation with other  
11      independent variables included in the model. Even if  
12      that correlation is zero, that is a measure of  
13      correlation. It simply has zero correlation. Any time  
14      an additional variable is included in a model, it will  
15      have impacts on the other regression coefficients for  
16      exactly the reason that they are correlated. That's the  
17      point of a multivariate regression, is to include  
18      additional variables that may be correlated with the  
19      original variable or with the other variables, because  
20      the researcher is interested in understanding what are  
21      called partial correlations. In other words, the impact  
22      of one variable independent of the impact of the other  
23      variables included in the model.

24           Q     Is there a point at which collinearity of  
25      regression variables becomes an issue such that it --

1 because it makes it hard to interpret the regression  
2 analysis?

3 A If two variables are perfectly correlated at 1,  
4 then it is impossible to include both of those variables  
5 in the regression. The regression will simply not work.  
6 It will not produce a result. Beyond that, it's a matter  
7 of -- it's a matter of degrees. It's a matter of -- and  
8 it's not simply a measure of how correlated the two  
9 variables are. It's a multidimensional problem and by  
10 problem, I don't mean that in a negative way. I mean,  
11 it's a multidimensional question and so there's a variety  
12 of factors that go into the results that you get from a  
13 regression, not just the correlation between two  
14 independent variables that you might be interested in  
15 including in your regression model.

16 Q So it sounds like you will not run a regression  
17 model using two independent variables that were perfectly  
18 correlated at 1; is that right?

19 A It can't be done.

20 Q So let's take the 0.96 correlation between  
21 Democratic vote share and BVAP in District 1. How would  
22 including those two -- if we take the 0.96 number as  
23 true, how does including those two independent variables  
24 in the same regression -- how would that affect the  
25 analysis?

1 MS. RIGGINS: Objection. Go ahead.

2 THE WITNESS: It's very hard to say. It's  
3 hard to know and the reason it's hard to know is  
4 because it not only depends on the correlation  
5 between those two variables, but it also depends on  
6 the particular values of individual data points. It  
7 depends on the correlation between those two  
8 variables and the other variables that are included  
9 in the model and it also depends on the correlation  
10 of those two variables with the outcome variable, the  
11 dependent variable. So it's a very multidimensional  
12 problem and, as a result, researchers don't -- you  
13 can't really know with certainty the impact it's  
14 having on your regression model. I guess I should  
15 say, you can't know without doing a variety of  
16 additional analyses.

17 Q You said earlier something about it being a  
18 matter of degree. So is it fair to say that if two  
19 independent variables are correlated at zero, there's no  
20 correlation, then there's no multicollinearity concern  
21 with including both in one regression model?

22 A Those variables could be correlated with other  
23 variables in the model, --

24 Q Right.

25 A -- but there is no multicollinearity if they're

1       not correlated with one another. So multicollinearity is  
2       a question of correlation between variables. So those  
3       variables could definitely have multicollinearity with  
4       other variables in the model, but they're not correlated  
5       with one another.

6           Q       Okay. And as a result, if you were to add an  
7       independent variable that was not correlated with any of  
8       the other existing independent variables, there would be  
9       no risk that adding that variable would introduce noise  
10      or variance that would be hard to understand?

11           MS. RIGGINS: Objection. Go ahead.

12           THE WITNESS: If you add in a variable that  
13       was completely exogenous, completely uncorrelated  
14       with any of the other independent variables, I still  
15       think that because that -- insofar as that variable  
16       is correlated with the dependent variable, it could  
17       also still have impact on the other independent  
18       variables in the model.

19           Q       Do you typically, when you are conducting  
20       regression analyses, try to minimize the number of  
21       independent variables that have high degrees of  
22       correlation with one another?

23           A       No. That's not usually a priority when you  
24       build a regression model.

25           Q       Once you kind of have run your regression and

1       gotten the various coefficients, is there anything that  
2       you can do to try to figure out whether multicollinearity  
3       affected those coefficients?

4           A      I suppose there are some measures that you can  
5       calculate to try and capture the degree to which they're  
6       correlated with one another or to capture the potential  
7       relationship that exists that you could conduct after  
8       running a regression model.

9           Q      What would that kind of like post-regression  
10      model analysis tell you?

11          A      It can tell you, one, the degree to which  
12       they're correlated. It could tell you the degree to  
13       which they're correlated in the context of all the other  
14       variables that are included in the model. It can give  
15       you an estimate of the variation or the variance, the  
16       variation that's induced in the model through the  
17       correlation. And then I guess the last thing is, what  
18       you're really estimating is the impact of the one  
19       variable on the outcome independent of the impact on the  
20       other variable on the outcome.

21          Q      Did you undertake that kind of check after  
22       running your regressions here?

23          A      I simply produced the regression results. So  
24       the results are telling us the relationship between the  
25       one variable independent of the other variable. These

1 additional post-regression diagnostics that I'm  
2 describing, I did not -- neither me nor Dr. Rodden  
3 produced those statistics.

4 Q Why didn't you produce those statistics here?

5 A I don't think that they are of particularly  
6 great value in this case because, regardless of what they  
7 say, we need to include both of those variables in the  
8 model. There's no value in running the regression with  
9 only a measure of race or only a measure of party.  
10 The only value that these regressions produce is when  
11 they're both included, because that is the question that  
12 we are seeking to answer, the impact of race independent  
13 of partisanship. If both variables are not included in  
14 the model, then the model is not getting us any closer to  
15 answering that question and at that point, why even  
16 bother including the model? It's not useful.

17 Q But it's possible that the model is also not  
18 useful if two of the variables are so highly correlated  
19 that it's basically meaningless?

20 MS. RIGGINS: Objection. Go ahead.

21 THE WITNESS: Well, I think I dispute the  
22 characterization of it as meaningless. No regression  
23 model is perfect. That's the nature of regression  
24 models. And so now it's a matter of which models are  
25 more informative or more helpful than others. And my

1                   opinion is that a model with partisanship and race  
2                   both included, even with the correlation that exists  
3                   between those two variables, is more valuable and is  
4                   more useful than a regression model that only  
5                   includes race or only includes partisanship. I do  
6                   not think that those models are really useful at all.

7                   Q        Let's flip back to your report. I just have a  
8                   few more questions and then we can consider whether it  
9                   makes sense to break for lunch. But if I go back to  
10                  page 18 of your report, you also mention at the end, to  
11                  account for the need to achieve relative population  
12                  parity, I also include a variable measuring the total  
13                  population of each precinct?

14                  A        Yes.

15                  Q        How does this control for population equality  
16                  in a district?

17                  A        What it accounts for is the fact that precincts  
18                  might -- stepping back, the purpose of the regression is  
19                  to identify what factors appear to be influential in the  
20                  selection of a precinct into a Congressional district.  
21                  One factor that's really important in creating  
22                  Congressional districts is population parity, and so when  
23                  a map drawer is deciding whether to move a precinct into  
24                  a district, one of the factors that they need to consider  
25                  is the population size of the precinct. So if you can

1 correlated.

2 Q Could you have undertaken your own correlation  
3 analysis?

4 A With sufficient time and resources, yes.

5 Q You applied the county envelope analysis to a  
6 set of simulated maps to test its reliability; is that  
7 right?

8 A Yes, that's correct.

9 Q And you also applied it to the  
10 2022 Special Master Map?

11 A I believe so, yes.

12 Q In doing so, did you run -- just to make sure  
13 I'm understanding, you ran your regression analysis. You  
14 ran the same regression analysis that you ran earlier in  
15 your report and you did not try to replicate Dr. Rodden's  
16 regression analysis on these simulated maps; is that  
17 correct?

18 A That's correct. I ran the same analysis that I  
19 conducted earlier in my report.

20 Q So that analysis includes both race and party  
21 as variables?

22 A Yes, it does.

23 Q And your opinion on page 27 of your report, at  
24 the bottom of this section, is that, given the results,  
25 it is my opinion that the envelope method is not a

1           reliable method for determining if race played a  
2           significant role in the assignment of precincts to  
3           districts; is that right?

4           A       Yes.

5           Q       And then turning to page 5 of your report,  
6           where you include a summary of conclusions, the second  
7           conclusion you list here is that the county envelope  
8           method is not a reliable method for examining the degree  
9           to which race played a role in the construction of  
10          district boundaries because it incorrectly identifies  
11          race as a significant factor when race, in fact, played  
12          no role in the process. What do you mean by the degree  
13          to which race played a role?

14          A       So in the simulations, the districts are  
15          constructed with no information about the racial  
16          composition of individual precincts or the state overall  
17          or the districts that are then assembled from those  
18          precincts. So we know ahead of time that race played no  
19          role in the development of these districts in the  
20          simulation. It was just not a factor that the computer  
21          had access to. And yet when we do the county envelope  
22          analysis, it identifies race as a statistically  
23          significant predictor of the district's composition more  
24          than a majority of the time, even though we knew ahead of  
25          time race played no factor in the composition of those

1 districts. So, in other words, the county envelope  
2 method, when applied to a truly race-neutral map, flags  
3 most of the districts as race playing a significant  
4 factor in the composition of the district. They're all  
5 false positives.

6 Q How are you determining whether your regression  
7 analysis is flagging race as a significant factor; what  
8 is the threshold that you're using there?

9 A So I'm using the same threshold that Dr. Rodden  
10 is using in the identification of the variable measuring  
11 race as whether or not it is statistically significant.

12 Q Just to confirm, when you refer here to the  
13 fact that race played no role in the process, you mean in  
14 reference to your simulated maps, correct?

15 A That's correct.

16 Q So you don't know, sitting here today, if race  
17 played any role in the 2023 redistricting, correct, in  
18 terms of, you're not speaking to the intent of the  
19 legislators?

20 A I don't have a view into the subjective intent  
21 of the people who drew the 2023 map.

22 Q And you're not opining here on whether the  
23 envelope method, used in combination with the other  
24 approaches that Dr. Rodden uses, can shed some light on  
25 whether racial sorting exists, correct?

1           A     Well, I'm opining that the county envelope  
2         method, in my opinion, sheds no light on whether race was  
3         a significant factor or not; and so I suppose that, in  
4         combination with other things, it provides no added value  
5         in my opinion.

6           Q     Okay. And just to make sure, so I'm not asking  
7         about whether race was a significant factor, but whether  
8         racial sorting exists at all. So not whether it was  
9         significant or what the intent was, but just rather  
10        whether there is racial sorting of the districts.

11          A     I suppose I don't fully understand what you  
12         mean by racial sorting.

13          Q     Whether voters are disproportionately included  
14         in a particular district or not, included based on their  
15         race. Setting aside whether their actual underlying  
16         reason might be their party or something like that, but  
17         just whether there exists any kind of effect that we can  
18         observe with respect to how voters are included or not  
19         included in districts based on their race.

20          A     I don't think the county envelope method is  
21         necessary to identify if there are differences in the  
22         regional composition of the districts. I think in that  
23         case, we can just look and see the summary statistics.  
24         The district has X percent of the district. X percent of  
25         the population are Black. That's something we can

1 identify without conducting any sort of county envelope  
2 analysis.

3 MS. JASRASARIA: I'm at a good stopping point  
4 if this is a good time to break for lunch.

5 THE WITNESS: Wonderful.

6 MS. JASRASARIA: Let's go off the record.

7 (There was a lunch recess taken.)

8 BY MS. JASRASARIA:

9 Q Welcome back, Dr. Barber.

10 A Thank you.

11 Q So I'd like to continue our discussion of your  
12 report. I'm going to share my screen again. So I'd like  
13 to turn to page 29 of your report, which is where you  
14 discuss the core-in-out analysis that Dr. Rodden  
15 conducted. Were you familiar with the core-in-out  
16 analysis before reviewing Dr. Rodden's report?

17 A Yes, I was familiar with it.

18 Q Where had you seen it before?

19 A I've seen it in -- I don't know that I could  
20 identify specific cases. I've been aware of it simply by  
21 virtue of being involved in redistricting cases, but more  
22 specifically, I'm aware of a similar -- it's not exactly  
23 this type of analysis, but a similar analysis that was  
24 done in a redistricting case that I am involved in, in  
25 Alabama.

1           A     Okay. So I think the first problem is you're  
2           making a comparison to a very small set of maps. 100  
3           maps is far outside the norm in terms of comparisons.  
4           Beyond that, this comparison is problematic for the same  
5           reasons that the analysis he does earlier is problematic,  
6           in that it does not disentangle race from partisanship.  
7           So he's suggesting here the plan is a racial outlier, but  
8           there's no analysis showing if this plan -- if the  
9           enacted map is also a partisan outlier, even in  
10          comparison to these 104 maps. Because these -- even  
11          though a map might have 10 Republican-leaning seats, if  
12          all 10 of those seats are just barely across the line, as  
13          we talked about at the very beginning this morning,  
14          that's different than if the 10 seats are beef-ly  
15          Republican. The analysis here and the figures here don't  
16          show us whether or not that is the case. It very well  
17          could be the case that there are no maps that have the  
18          same partisan composition as the enacted map in terms of  
19          not only the number of Republican-leaning seats but the  
20          relative safety of those seats.

21           Q     Did you review the draft maps that Dr. Rodden  
22          included in his reply report analysis?

23           A     I have not.

24           Q     Do you have any reason to dispute the BVAP  
25          distribution that he showed in his analysis?

1           A     I have not -- I have not looked at these draft  
2       maps. I don't know -- I couldn't say anything about  
3       these draft maps at this point.

4           Q     Let me stop sharing my screen for a moment.  
5       Dr. Barber, what is your understanding of how a Court  
6       determines whether a district is a racial gerrymander?

7           MS. RIGGINS: Objection. Go ahead.

8           THE WITNESS: I don't know that I can answer  
9       that question. I think that a judge makes that  
10      decision and I don't really know how a judge makes  
11      that determination.

12          Q     Are you familiar with the concept of racial  
13      predominance?

14          A     I'm familiar with the phrase, yes.

15          Q     What is your understanding of what that phrase  
16      means?

17          A     I think that it has -- I think that phrase has  
18      a kind of special legal standing or kind of legal --  
19      lawyers have a very different -- like, a special  
20      definition of what that means. I'm not trying to  
21      describe what that is, because I'm not a lawyer and I'm  
22      not making any sort of legal determinations. In my  
23      own -- sorry, go ahead.

24          Q     No, go for it.

25          A     In my own non-legal understanding, I think